

The birth of a convention (scalarity and context)

A history lesson

In times of old, contexts were scalar, and so were calculandi. By way of example, take C as scalar context, and P as scalar calculandum.

The English phrases “ P holds” or “we have P ” were then, by convention, shorthand for:

$$(0) \quad C \Rightarrow P \quad .$$

And please note that:

“(0) makes sense as an English proposition”

$$\equiv \{ \quad \}$$

“(0) is scalar”

$$\equiv \{ \quad \}$$

“ C is scalar” \wedge “ P is scalar” $\quad .$

So back in times of old, if you were to drop the condition of scalarity on either C or P , then a phrase like “ P holds (in context C)” would be treated as uninterpretable.

Adapting to the times

What a nice history lesson. However, times are changing, and in particular, contexts and calculandi are structures as often as they are scalars. So towards that end, let’s generalize convention (0), where by “generalize” I mean that the generalized convention should work for structures, but should also reduce to the original convention when C and P are scalar.

We calculate:

$$C \Rightarrow P$$

$$\equiv \{ P \text{ is scalar} \}$$

$$C \Rightarrow [P]$$

$$\equiv \{ C \text{ is scalar} \}$$

$$[C \Rightarrow P] \quad .$$

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And so we have derived:

$$(1) \quad [C \Rightarrow P]$$

as an equivalent way of formulating (0) and “ P holds (in context C)”, when C and P are scalar.

But please observe that formulation (1) is more general, because it makes sense as an English proposition even when C and P are structures.

Thus we find that “ P holds (in context C)” ought to stand for (1) .

And there you have the birth of a convention.

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